

# Unfolding of symmetric monoidal $(\infty, n)$ -categories

R. Haugseng

**Rune Haugseng** ([rune.haugsens@ntnu.no](mailto:rune.haugsens@ntnu.no))  
Norwegian University of Science and Technology (NTNU)

**Thomas Nikolaus** ([nikolaus@uni-muenster.de](mailto:nikolaus@uni-muenster.de))  
University of Münster

## Abstract.

In Lurie’s article on the Cobordism Hypothesis [1], he discusses a description of symmetric monoidal  $(\infty, n)$ -categories with duals for objects and certain adjoints as “chain complexes” of symmetric monoidal  $\infty$ -categories with duals, but does not give a proof. This gives a surprisingly simple description of symmetric monoidal  $(\infty, n)$ -categories with duals that should be useful both in connection with extended TQFTs and in stable homotopy theory. We will give a proof of this “unfolding” equivalence in forthcoming work, based on a general description of closed symmetric monoidal  $\mathcal{V}$ -enriched  $\infty$ -categories as lax symmetric monoidal functors to  $\mathcal{V}$ . In this talk I will explain how this comparison works, focusing on the simplest cases (for  $n = 2$  and  $3$ ).

## References

- [1] J. Lurie, *On the classification of topological field theories*, Current developments in mathematics, 2008, Int. Press, Somerville, MA, 2009, pp. 129–280, available at <http://math.ias.edu/~lurie/papers/cobordism.pdf>.